

# Package ‘orderedLasso’

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**Title** Ordered Lasso and Time-Lag Sparse Regression

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**Description** Ordered lasso and time-lag sparse regression. Ordered Lasso fits a linear model and imposes an order constraint on the coefficients. It writes the coefficients as positive and negative parts, and requires positive parts and negative parts are non-increasing and positive. Time-Lag Lasso generalizes the ordered Lasso to a general data matrix with multiple predictors. For more details, see Suo, X., Tibshirani, R., (2014) 'An Ordered Lasso and Sparse Time-lagged Regression'.

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 orderedLasso

*Fit an ordered lasso*


---

### Description

One of the main functions. Ordered Lasso builds a regression model with an L1-constraint imposed on the coefficients. The coefficients are re-written as negative and positive parts and the model requires positive and negative parts are monotone non-increasing and positive.

### Usage

```
orderedLasso(x, y, lambda, intercept = TRUE, b0 = NULL, beta_pos = NULL,
  beta_neg = NULL, method = c("Solve.QP", "GG"), strongly.ordered = FALSE,
  standardize = TRUE, trace = FALSE, niter = 500, iter.gg = 100,
  epsilon = 1e-08)
```

### Arguments

x	A matrix of predictors, where the rows are the samples and the columns are the predictors
y	A vector of observations, where length(y) equals nrow(x)
lambda	Regularization parameter(>0)
intercept	TRUE if there is an intercept in the model.
b0	Initial value for the intercept.
beta_pos	Optional vector of initialization of the positive part of the coefficients.
beta_neg	Optional vector of initialization of the negative part of the coefficients.
method	Two options available, Solve.QP and Generalized Gradient. Solve.QP uses the package quadprog to solve a quadratic programming problem. GG stands for generalizable gradient. GG uses proximal generalizable gradient algorithm to solve the problem. Detailed can be seen in the paper referred in the description.
strongly.ordered	An option which allows users to order the coefficients in absolute value. The coefficients returned by the orderedLasso may not be monotone non-increasing in absolute value even though the positive parts and negative parts are monotone non-increasing. Details can be seen in the paper referred in the Description. Strongly.ordered options returns the coefficients monotone non-increasing in absolute value.
standardize	Standardize the data matrix x
trace	Output option; trace = TRUE gives verbose output
niter	Maximum number of iterations; default 500.
iter.gg	Number of iterations of generalizable gradient; default 100
epsilon	Error tolerance parameter for convergence criterion ; default 1e-05.

**Value**

bp	Estimated coefficients- positive part
bn	Estimated coefficients- negative part
beta	Estimated coefficients, which are equal to bp - bn
b0	Estimated intercept, if there is one in the model.
fitted	Fitted values of y
type	Type of model fit, "gaussian"
call	The call to orderedLasso

**Examples**

```

set.seed(3)
n = 50
b = c(7,3,1,0)
p = length(b)
x = matrix(rnorm(n*p),nrow = n)
sigma = 4
y = x %*% b + sigma * rnorm(n, 0, 1)
result1 = orderedLasso(x,y, lambda = 1, intercept =TRUE, standardize = TRUE,
  method = "GG", strongly.ordered = TRUE)
result2 = orderedLasso(x,y, lambda = 1, intercept = TRUE, standardize =TRUE,
  strongly.ordered = TRUE)
print(result1)
print(result2)

```

---

orderedLasso.cv

*Cross-validation function for the ordered lasso*


---

**Description**

Uses cross-validation to estimate the regularization parameter for the ordered lasso model.

**Usage**

```

orderedLasso.cv(x, y, lamlist = NULL, minlam = NULL, maxlam = NULL,
  nlam = 50, flmin = 5e-04, strongly.ordered = FALSE, intercept = TRUE,
  standardize = TRUE, nfolds = 10, folds = NULL, niter = 500,
  iter.gg = 100, method = c("Solve.QP", "GG"), trace = FALSE,
  epsilon = 1e-05)

```

**Arguments**

x	A matrix of predictors, where the rows are the samples and the columns are the predictors
y	A vector of observations, where length(y) equals nrow(x)

lamlist	Optional vector of values of lambda (the regularization parameter)
minlam	Optional minimum value for lambda
maxlam	Optional maximum value for lambda
nlam	Number of values of lambda to be tried. Default nlam = 50.
flmin	Fraction of maxlam minlam= flmin*maxlam. If computation is slow, try increasing flmin to focus on the sparser part of the path. Default flmin = 1e-4.
strongly.ordered	An option which allows users to order the coefficients in absolute value.
intercept	True if there is an intercept in the model.
standardize	Standardize the data matrix.
nfolds	Number of cross-validation folds.
folds	(Optional) user-supplied cross-validation folds. If provided, nfolds is ignored.
niter	Number of iterations the ordered lasso takes to converge. Default niter = 500.
iter.gg	Number of iterations of generalized gradient method; default 100
method	Two options available, Solve.QP and Generalized Gradient. Details of two options can be seen in the orderedLasso description.
trace	Output option; trace=TRUE gives verbose output
epsilon	Error tolerance parameter for convergence criterion; default 1e-5

### Examples

```

set.seed(3)
n = 50
b = c(4,3,1,0)
p = length(b)
x = matrix(rnorm(n*p),nrow = n)
sigma = 5
y = x %*% b + sigma * rnorm(n, 0, 1)
cvmodel = orderedLasso.cv(x,y, intercept = FALSE, trace = TRUE,
                          method = "Solve.QP", strongly.ordered = TRUE)
print(cvmodel)
plot(cvmodel)

```

---

orderedLasso.path      *Fit a path of ordered lasso models*

---

### Description

Fit a path of ordered lasso models over different values of the regularization parameter.

### Usage

```

orderedLasso.path(x, y, lamlist = NULL, minlam = NULL, maxlam = NULL,
                 nlam = 50, flmin = 0.005, intercept = TRUE, standardize = TRUE,
                 method = c("Solve.QP", "GG"), niter = 500, iter.gg = 100,
                 strongly.ordered = FALSE, trace = FALSE, epsilon = 1e-05)

```

**Arguments**

x	A matrix of predictors, where the rows are the samples and the columns are the predictors
y	A vector of observations, where length(y) equals nrow(x)
lamlist	Optional vector of values of lambda (the regularization parameter)
minlam	Optional minimum value for lambda
maxlam	Optional maximum value for lambda
nlam	Number of values of lambda to be tried. Default nlam = 50
fmin	Fraction of maxlam; minlam= fmin*maxlam. If computation is slow, try increasing fmin to focus on the sparser part of the path
intercept	True if there is an intercept in the model.
standardize	Standardize the data matrix x. Default is TRUE.
method	Two options available, Solve.QP and Generalized Gradient.
niter	Number of iterations of ordered lasso, initialized to 500.
iter.gg	Number of iterations of genealized gradient; Default iter.gg = 100
strongly.ordered	An option which allows users to order the coefficients non-decreasing in absolute value. Details can be seen in the orderedLasso Description.
trace	Output option; trace=TRUE gives verbose output
epsilon	Error tolerance parameter for convergence criterion. Default is 1e-5

**Value**

bp	p by nlam matrix of estimated positive coefficients(p=#variables)
bn	p by nlam matrix of estimated negative coefficients
beta	p by nlam matrix of estimated coefficients
b0	a length nlam vector of estimated intercepts
lamlist	Vector of values of lambda used
err	Vector of errors
call	The call to orderedLasso.path

**Examples**

```

set.seed(3)
n = 50
b = c(4,3,1,0)
p = length(b)
x = matrix(rnorm(n*p),nrow = n)
sigma = 5
y = x %*% b + sigma * rnorm(n, 0, 1)
path1 = orderedLasso.path(x,y, intercept = FALSE,
  method = "Solve.QP", strongly.ordered = TRUE)
plot(path1)
print(path1)

```

---

predict.orderedLasso    *make predictions from a fitted "orderedLasso" object*

---

### Description

Similar to other predict methods, this functions predicts fitted values from a fitted "orderedLasso" object.

### Usage

```
## S3 method for class 'orderedLasso'
predict(object, newdata, ...)
```

### Arguments

object	fitted "orderedLasso" model
newdata	Matrix of new values for object at which predictions are to be made.
...	Not used. Other arguments to predict.

### Value

yhat	fitted y values
------	-----------------

---

predict.orderedLasso.path  
                                   *make predictions from a fitted "orderedLasso.path" object*

---

### Description

Similar to other predict methods, this functions predicts fitted values from a fitted "orderedLasso" object.

### Usage

```
## S3 method for class 'orderedLasso.path'
predict(object, newdata, s = NULL,
        exact = FALSE, ...)
```

**Arguments**

object	fitted "orderedLasso.path" model
newdata	Matrix of new values for object at which predictions are to be made.
s	Value(s) of the penalty parameter lambda at which predictions are required. Default is the entire sequence used to create the model.
exact	If exact = TRUE, and predictions are to be made at values of s not included in the original fit, these values of s are merged with object\$lambda, and the model is refit before predictions are made. If exact = FALSE (default), then the predict function uses linear interpolation to make predictions for values of s that do not coincide with those used in the fitting algorithm. Note that exact = TRUE is fragile when used inside a nested sequence of function calls. predict.orderedLasso() needs to update the model, and expects the data used to create it to be around.
...	Not used. Other arguments to predict.

**Value**

nfit	A matrix or a vector of fitted values
------	---------------------------------------

---

predict.timeLagLasso *make predictions from a fitted "timeLagLasso" object*

---

**Description**

Similar to other predict methods, this functions predicts fitted values from a fitted "timeLagLasso" object.

**Usage**

```
## S3 method for class 'timeLagLasso'
predict(object, newdata = NULL, ...)
```

**Arguments**

object	fitted "timeLagLasso" model
newdata	Matrix of new values for object at which predictions are to be made.
...	Not used. Other arguments to predict.

**Value**

yhat	fitted y values
yhat.ordered	fitted y values of the strongly ordered coefficients

---

```
predict.timeLagLasso.path
```

*make predictions from a fitted "timeLagLasso.path" object*

---

### Description

Similar to other predict methods, this functions predicts fitted values from a fitted "timeLagLasso.path" object.

### Usage

```
## S3 method for class 'timeLagLasso.path'
predict(object, newdata = NULL, s = NULL,
        exact = FALSE, ...)
```

### Arguments

object	fitted "timeLagLasso.path" model
newdata	Matrix of new values for object at which predictions are to be made.
s	Value(s) of the penalty parameter lambda at which predictions are required. Default is the entire sequence used to create the model.
exact	If exact = TRUE, and predictions are to made at values of s not included in the original fit, these values of s are merged with object\$lambda, and the model is refit before predictions are made. If exact = FALSE (default), then the predict function uses linear interpolation to make predictions for values of s that do not coincide with those used in the fitting algorithm. Note that exact = TRUE is fragile when used inside a nested sequence of function calls. predict.orderedLasso() needs to update the model, and expects the data used to create it to be around.
...	Not used. Other arguments to predict.

### Value

yhat	A matrix or a vector of fitted values
yhat.ordered	A matrix or a vector of fitted values of the strongly ordered lasso coefficients

---

```
timeLagLasso
```

*Fit a time-lag lasso*

---

### Description

Fit a time-lag lasso model. Builds a regression model with multiple predictors, where an ordered constraint is imposed on each predictor.



**Usage**

```
timeLagLasso(x, y, lambda, maxlag, intercept = TRUE, standardize = TRUE,
  beta_pos = NULL, beta_neg = NULL, b0 = NULL, strongly.ordered = TRUE,
  maxiter = 500, inneriter = 100, iter.gg = 100, method = c("Solve.QP",
  "GG"), trace = FALSE, epsilon = 1e-05)
```

**Arguments**

x	A matrix of predictors, where the rows are the samples and the columns are the predictors.
y	A vector of observations, where length(y) equals nrow(x).
lambda	Regularization parameter(>0).
maxlag	maximum time-lag specified by user.
intercept	TRUE if there is an intercept in the model. center=FALSE should almost never be used. This option is available for special uses only.
standardize	Standardize the data matrix x.
beta_pos	Optional vector of initialization of the positive part of the coefficients.
beta_neg	Optional vector of initialization of the negative part of the coefficients.
b0	Initialization of the intercept.
strongly.ordered	An option which allows users to order each predictor coefficients non-increasing in absolute value. Details can be seen in the orderedLasso description; default TRUE.
maxiter	Maximum iterations run by time-lag lasso. Initialized to 500.
inneriter	Maximum iterations run by orderedLasso. Initialized to 100.
iter.gg	Maximum iterations run by generalized gradient. Intialized to 100
method	Two options available, Solve.QP and Generalized Gradient
trace	Output option; trace = TRUE gives verbose output.
epsilon	Error tolerance parameter for convergence criterion; default 1e-5.

**Details**

First transfer the data matrix x to the correct format corresponding to the maxlag specified by user. Then use coordinate descent method by calling orderedLasso to get updates for each predictor.

**Value**

bp	Estimated coefficients of the positive part
bn	Estimated coefficients of the negative part
beta	Estimated coefficients of predictors, which are equal to bp - bn
b0	Estimated intercept if there is one in the model
fitted	Fitted values of y
maxlag	Maximum time-lag
p	The number of predictors
type	Type of model fit, "gaussian" in this case

**Examples**

```

set.seed(3)
n = 50
maxlag = 5
num_rows_needed = n + maxlag + 1
sigma = 4
x = matrix(rnorm(num_rows_needed * 4), nrow = num_rows_needed)
x_new = time_lag_matrix(x, maxlag)
b = c(3,1,1,0,0,
      4,1,0,0,0,
      3,2,1,0,0,
      1,0,0,0,0)
y = x_new %*% b + sigma* rnorm(nrow(x_new))
y = as.vector(y)
y = c(y, rnorm(maxlag + 1))
model1 = timeLagLasso(x = x, y = y, lambda = 1, maxlag = maxlag,
                     method = "Solve.QP", strongly.ordered = TRUE)

```

timeLagLasso.cv

*Cross-validation function for timeLagLasso***Description**

Uses cross-validation to estimate the regularization parameter for timeLagLasso model

**Usage**

```

timeLagLasso.cv(x, y, maxlag, lamlist = NULL, minlam = NULL,
               maxlam = NULL, nlam = 10, flmin = 0.01, flmax = 1, intercept = TRUE,
               standardize = TRUE, method = c("Solve.QP", "GG"),
               strongly.ordered = TRUE, nfolds = 10, folds = NULL, maxiter = 500,
               inneriter = 100, iter.gg = 100, trace = FALSE, epsilon = 1e-04)

```

**Arguments**

x	A matrix of predictors, where the rows are the samples and the columns are the predictors
y	A vector of observations, where length(y) equals nrow(x)
maxlag	Maximum time-lag variable chosen by user
lamlist	Optional vector of values of lambda (the regularization parameter)
minlam	Optional minimum value for lambda
maxlam	Optional maximum value for lambda
nlam	Number of values of lambda to be tried
flmin	Fraction of maxlam minlam= flmin*maxlam. If computation is slow, try increasing flmin to focus on the sparser part of the path; default 1e-2

f1max	Multiplication of maxlam $\text{maxlam} = \text{f1max} * \text{maxlam}$ ; default 1
intercept	True if there is an intercept in the model.
standardize	Standardize the data matrix x.
method	Two options available, Solve.QP and Generalized Gradient. Details about two options can be seen in the orderedLasso description.
strongly.ordered	An option which allows users to order the coefficients in absolute value.
nfolds	Number of cross-validation folds
folds	(Optional) user-supplied cross-validation folds. If provided, nfolds is ignored.
maxiter	maximum iterations run by time-lag lasso. Initialized to 500.
inneriter	maximum iterations run by orderedLasso. Initialized to 100.
iter.gg	Maximum iterations run by generalized gradient. Intialized to 100
trace	Output option; trace = TRUE gives verbose output.
epsilon	Error tolerance parameter for convergence criterion; default 1e-5

**Value**

lamlist	Vector of lambda values tried
cv.err	Estimate of cross-validation error
cv.se	Estimated standard error of cross-validation estimate
lamhat	lambda value minimizing cv.err
folds	Indices of folds used in cross-validation
lamhat.1se	largest lambda value with cv.err less than or equal to $\min(\text{cv.err}) + \text{SE}$
nonzero	Vector giving number of non-zero coefficients for each lambda value
call	The call to timeLagLasso.cv

**Examples**

```

set.seed(3)
n = 50
maxlag = 5
num_rows_needed = n + maxlag + 1
sigma = 4
x = matrix(rnorm(num_rows_needed * 4), nrow = num_rows_needed)
x_new = time_lag_matrix(x, maxlag)
b = c(3,1,1,0,0,
      4,1,0,0,0,
      3,2,1,0,0,
      1,0,0,0,0)
y = x_new %*% b + sigma* rnorm(nrow(x_new))
y = as.vector(y)
y = c(y, rnorm(maxlag + 1))
cvmodel = timeLagLasso.cv(x= x, y = y, maxlag = 5, method = "Solve.QP")

```

---

timeLagLasso.path      *Fit a path of time-lasso models*

---

## Description

Fit a path of time-lasso models

## Usage

```
timeLagLasso.path(x, y, lamlist = NULL, minlam = NULL, maxlam = NULL,
  nlam = 10, flmin = 0.01, strongly.ordered = TRUE, flmax = 1, maxlag,
  intercept = TRUE, standardize = TRUE, method = c("Solve.QP", "GG"),
  maxiter = 500, inneriter = 100, iter.gg = 100, trace = FALSE,
  epsilon = 1e-05)
```

## Arguments

x	A matrix of predictors, where the rows are the samples and the columns are the predictors
y	A vector of observations, where length(y) equals nrow(x)
lamlist	Optional vector of values of lambda (the regularization parameter)
minlam	Optional minimum value for lambda
maxlam	Optional maximum value for lambda
nlam	Number of values of lambda to be tried
flmin	Fraction of maxlam minlam= flmin*maxlam. If computation is slow, try increasing flmin to focus on the sparser part of the path; default = 1e-2.
strongly.ordered	An option which allows users to order the coefficients in absolute value.
flmax	Multiplication of maxlam maxlam = flmax * maxlam. Default = 1
maxlag	Maximum time-lag chosen by user.
intercept	True if there is an intercept in the model.
standardize	Standardize the data matrix x.
method	Two options available, Solve.QP and Generalized Gradient
maxiter	Maximum iterations run by time-lag lasso. Initiazlied to 500.
inneriter	maximum iterations run by orderedLasso. Initialized to 100.
iter.gg	Maximum iterations run by generalized gradient. Intialized to 100
trace	Output option; trace = TRUE gives verbose output.
epsilon	Error tolerance parameter for convergence criterion; default 1e-5

**Value**

bp	p by nlam matrix of estimated positive coefficients(p=#variables)
bn	p by nlam matrix of estimated negative coefficients
beta	p by nlam matrix of estimated coefficients
b0	a vector of length nlam of estimated intercept
lamlist	Vector of values of lambda used
err	Vector of errors
maxlag	Maximum time-lag variable
p	The number of predictors
fited	a length(y) by nlam matrix of fitted values
call	The call to "timeLagLasso.path"

**Examples**

```

set.seed(3)
n = 50
maxlag = 5
num_rows_needed = n + maxlag + 1
sigma = 4
x = matrix(rnorm(num_rows_needed * 4), nrow = num_rows_needed)
x_new = time_lag_matrix(x, maxlag)
b = c(3,1,1,0,0,
      4,1,0,0,0,
      3,2,1,0,0,
      1,0,0,0,0)
y = x_new %*% b + sigma* rnorm(nrow(x_new))
y = as.vector(y)
y = c(y, rnorm(maxlag + 1))
path1 = timeLagLasso.path(x= x, y = y, maxlag = 5, method = "Solve.QP", strongly.ordered = TRUE)
plot(path1)

```

---

time\_lag\_matrix      *time\_lag\_matrix*

---

**Description**

Build the time lag matrix for the data matrix x.

**Usage**

```
time_lag_matrix(x, maxlag)
```

**Arguments**

x	A matrix of predictors, where the rows are the samples and the columns are the predictors
maxlag	maximum time lag variable.

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