

Twin analysis

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Mets package

This document provides a brief tutorial to analyzing twin data using the `mets` package:

```
1 library("mets")
2 options(warn=-1)
```

The development version may be installed from *github*, i.e., with the `devtools` package:

```
1 devtools::install_github("kkholst/lava")
2 devtools::install_github("kkholst/mets")
```

Twin analysis, continuous traits

In the following we examine the heritability of Body Mass Index^{1 2}, based on data on self-reported BMI-values from a random sample of 11,411 same-sex twins. First, we will load data

```
1 data("twinbmi")
2 head(twinbmi)
```

	tvparnr	bmi	age	gender	zyg	id	num
1	1	26.33289	57.51212	male	DZ	1	1
2	1	25.46939	57.51212	male	DZ	1	2
3	2	28.65014	56.62696	male	MZ	2	1
5	3	28.40909	57.73097	male	DZ	3	1
7	4	27.25089	53.68683	male	DZ	4	1
8	4	28.07504	53.68683	male	DZ	4	2

The data is on *long* format with one subject per row. we transpose the data allowing us to do pairwise analyses

```
1 twinwide <- fast.reshape(twinbmi, id="tvparnr", varying=c("
  bmi"))
2 head(twinwide)
```

	tvparnr	bmi1	age	gender	zyg	id	num	bmi2
1	1	26.33289	57.51212	male	DZ	1	1	25.46939
3	2	28.65014	56.62696	male	MZ	2	1	NA
5	3	28.40909	57.73097	male	DZ	3	1	NA
7	4	27.25089	53.68683	male	DZ	4	1	28.07504
9	5	27.77778	52.55838	male	DZ	5	1	NA
11	6	28.04282	52.52231	male	DZ	6	1	22.30936

Next we plot the association within each zygosity group

¹ M. Korkeila, J. Kaprio, A. Rissanen, and M. Koskenvuo. Effects of gender and age on the heritability of body mass index. *Int J Obes*, 15(10):647–654, Oct 1991

² J. v. Hjelmborg, C. Fagnani, K. Silventoinen, M. McGue, M. Korkeila, K. Christensen, A. Rissanen, and J. Kaprio. Genetic influences on growth traits of BMI: a longitudinal study of adult twins. *Obesity (Silver Spring)*, 16(4):847–852, Apr 2008

`tvparnr` twin id

`bmi` Body Mass Index (kg/m²)

`age` Age (years)

`gender` Gender factor (male,female)

`zyg` zygosity (MZ,DZ)

```

1 library("cowplot")
2
3 scatterdens <- function(x) {
4   sp <- ggplot(x,
5     aes_string(colnames(x)[1], colnames(x)[2])) +
6     theme_minimal() +
7     geom_point(alpha=0.3) + geom_density_2d()
8   xdens <- ggplot(x, aes_string(colnames(x)[1],fill=1)) +
9     theme_minimal() +
10    geom_density(alpha=.5)+
11    theme(axis.text.x = element_blank(),
12      legend.position = "none") + labs(x=NULL)
13   ydens <- ggplot(x, aes_string(colnames(x)[2],fill=1)) +
14     theme_minimal() +
15     geom_density(alpha=.5) +
16     theme(axis.text.y = element_blank(),
17       axis.text.x = element_text(angle=90, vjust=0),
18       legend.position = "none") +
19     labs(x=NULL) +
20     coord_flip()
21   g <- plot_grid(xdens,NULL,sp,ydens,
22     ncol=2,nrow=2,
23     rel_widths=c(4,1.4),rel_heights=c(1.4,4))
24   return(g)
25 }

```

We here show the log-transformed data which is slightly more symmetric and more appropriate for the twin analysis (see Figure 1 and 2)

```

1 mz <- log(subset(twinwide, zyg=="MZ"),c("bmi1", "bmi2"))
2 scatterdens(mz)

```

```

1 dz <- log(subset(twinwide, zyg=="DZ"),c("bmi1", "bmi2"))
2 scatterdens(dz)

```

The plots and raw association measures shows considerable stronger dependence in the MZ twins, thus indicating genetic influence of the trait

```

1 cor.test(mz[,1],mz[,2], method="spearman")

```

Spearman's rank correlation rho

```

data: mz[, 1] and mz[, 2]
S = 165460000, p-value < 2.2e-16
alternative hypothesis: true rho is not equal to 0
sample estimates:
rho
0.6956209

```

```

1 cor.test(dz[,1],dz[,2], method="spearman")

```

Spearman's rank correlation rho

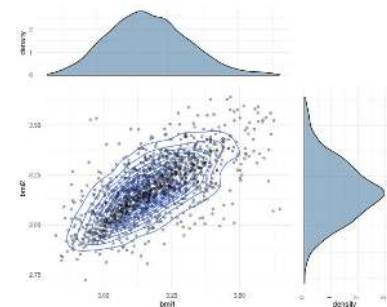


Figure 1: Scatter plot of logarithmic BMI measurements in MZ twins.

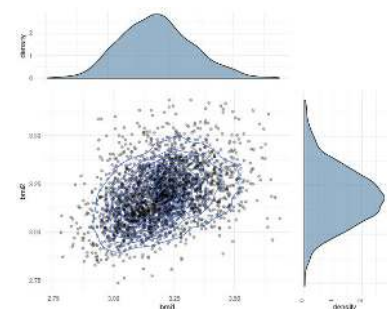


Figure 2: Scatter plot of logarithmic BMI measurements in DZ twins.

```

data: dz[, 1] and dz[, 2]
S = 2162500000, p-value < 2.2e-16
alternative hypothesis: true rho is not equal to 0
sample estimates:
      rho
0.4012686

```

Next we examine the marginal distribution (GEE model with working independence)

```

1 l0 <- lm(bmi ~ gender + I(age-40), data=twinbmi)
2 estimate(l0, id=twinbmi$tvparnr)

```

	Estimate	Std.Err	2.5%	97.5%	P-value
(Intercept)	23.3687	0.054534	23.2618	23.4756	0.000e+00
gendermale	1.4077	0.073216	1.2642	1.5512	2.230e-82
I(age - 40)	0.1177	0.004787	0.1083	0.1271	1.499e-133

```

1 library("splines")
2 l1 <- lm(bmi ~ gender*ns(age,3), data=twinbmi)
3 marg1 <- estimate(l1, id=twinbmi$tvparnr)

```

```

1 dm <- Expand(twinbmi,
2   bmi=0,
3   gender=c("male"),
4   age=seq(33,61,length.out=50))
5 df <- Expand(twinbmi,
6   bmi=0,
7   gender=c("female"),
8   age=seq(33,61,length.out=50))
9
10 plot(marg1, function(p) model.matrix(l1,data=dm)%*%p,
11   data=dm["age"], ylab="BMI", xlab="Age",
12   ylim=c(22,26.5))
13 plot(marg1, function(p) model.matrix(l1,data=df)%*%p,
14   data=df["age"], col="red", add=TRUE)
15 legend("bottomright", c("Male","Female"),
16   col=c("black","red"), lty=1, bty="n")

```

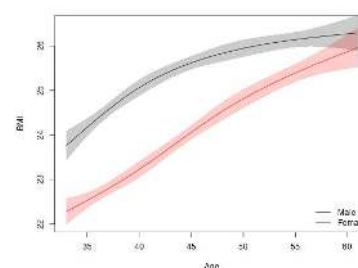


Figure 3: ...

Polygenic model

Decompose outcome into

$$Y_i = A_i + D_i + C + E_i, \quad i = 1, 2$$

A Additive genetic effects of alleles

D Dominant genetic effects of alleles

C Shared environmental effects

E Unique environmental genetic effects

Dissimilarity of MZ twins arises from unshared environmental effects only! $\text{Cor}(E_1, E_2) = 0$ and

$$\text{Cor}(A_1^{MZ}, A_2^{MZ}) = 1, \quad \text{Cor}(D_1^{MZ}, D_2^{MZ}) = 1,$$

$$\text{Cor}(A_1^{DZ}, A_2^{DZ}) = 0.5, \quad \text{Cor}(D_1^{DZ}, D_2^{DZ}) = 0.25,$$

$$Y_i = A_i + C_i + D_i + E_i$$

$$A_i \sim \mathcal{N}(0, \sigma_A^2), C_i \sim \mathcal{N}(0, \sigma_C^2), D_i \sim \mathcal{N}(0, \sigma_D^2), E_i \sim \mathcal{N}(0, \sigma_E^2)$$

$$\text{Cov}(Y_1, Y_2) =$$

$$\begin{pmatrix} \sigma_A^2 & 2\Phi\sigma_A^2 \\ 2\Phi\sigma_A^2 & \sigma_A^2 \end{pmatrix} + \begin{pmatrix} \sigma_C^2 & \sigma_C^2 \\ \sigma_C^2 & \sigma_C^2 \end{pmatrix} + \begin{pmatrix} \sigma_D^2 & \Delta_7\sigma_D^2 \\ \Delta_7\sigma_D^2 & \sigma_D^2 \end{pmatrix} + \begin{pmatrix} \sigma_E^2 & 0 \\ 0 & \sigma_E^2 \end{pmatrix}$$

```

1 dd <- na.omit(twinbmi)
2 lo <- twinlm(bmi ~ age+gender, data=dd,
3             DZ="DZ", zyg="zyg", id="tvparnr", type="sat")

```

```

1 l <- twinlm(bmi ~ ns(age,1)+gender, data=twinbmi,
2             DZ="DZ", zyg="zyg", id="tvparnr", type="cor", missing=
3             TRUE)
4 summary(l)

```

```

-----
Group 1

```

	Estimate	Std. Error	Z value	Pr(> z)
Regressions:				
bmi.1~ns(age, 1).1	4.16937	0.16669	25.01334	<1e-12
bmi.1~gendermale.1	1.41160	0.07284	19.37839	<1e-12
Intercepts:				
bmi.1	22.53618	0.07296	308.87100	<1e-12
Additional Parameters:				
log(var)	2.44580	0.01425	171.68256	<1e-12
atanh(rhoMZ)	0.78217	0.02290	34.16186	<1e-12

```

-----
Group 2

```

	Estimate	Std. Error	Z value	Pr(> z)
Regressions:				
bmi.1~ns(age, 1).1	4.16937	0.16669	25.01334	<1e-12
bmi.1~gendermale.1	1.41160	0.07284	19.37839	<1e-12
Intercepts:				
bmi.1	22.53618	0.07296	308.87100	<1e-12
Additional Parameters:				
log(var)	2.44580	0.01425	171.68256	<1e-12
atanh(rhoDZ)	0.29924	0.01848	16.19580	<1e-12

```


```

	Estimate	2.5%	97.5%
Correlation within MZ:	0.65395	0.62751	0.67889
Correlation within DZ:	0.29061	0.25712	0.32341

```

'log Lik.' -29020.12 (df=6)
AIC: 58052.24
BIC: 58093.29

```

A formal test of genetic effects can be obtained by comparing the MZ and DZ correlation:

```

1 estimate(1, contr(5:6,6))

```

```

                Estimate Std.Err   2.5%  97.5%  P-value
[atanh(rhoMZ)@1] - [a...   0.4829 0.04176 0.4011 0.5648 6.325e-31

```

Null Hypothesis:

```
[atanh(rhoMZ)@1] - [atanh(rhoDZ)@3] = 0
```

```

1 l <- twinlm(bmi ~ ns(age,1)+gender, data=twinbmi,
2           DZ="DZ", zyg="zyg", id="tvparnr", type="cor", missing=
           TRUE)
3 summary(l)

```

```

-----
Group 1
                Estimate Std. Error   Z value Pr(>|z|)
Regressions:
  bmi.1~ns(age, 1).1  4.16937   0.16669  25.01334 <1e-12
  bmi.1~gendermale.1  1.41160   0.07284  19.37839 <1e-12
Intercepts:
  bmi.1              22.53618   0.07296 308.87100 <1e-12
Additional Parameters:
  log(var)           2.44580   0.01425 171.68256 <1e-12
  atanh(rhoMZ)       0.78217   0.02290  34.16186 <1e-12

```

```

-----
Group 2
                Estimate Std. Error   Z value Pr(>|z|)
Regressions:
  bmi.1~ns(age, 1).1  4.16937   0.16669  25.01334 <1e-12
  bmi.1~gendermale.1  1.41160   0.07284  19.37839 <1e-12
Intercepts:
  bmi.1              22.53618   0.07296 308.87100 <1e-12
Additional Parameters:
  log(var)           2.44580   0.01425 171.68256 <1e-12
  atanh(rhoDZ)       0.29924   0.01848  16.19580 <1e-12

```

```

                Estimate 2.5%   97.5%
Correlation within MZ: 0.65395 0.62751 0.67889
Correlation within DZ: 0.29061 0.25712 0.32341

```

```

'log Lik.' -29020.12 (df=6)
AIC: 58052.24
BIC: 58093.29

```

Twin analysis, censored outcomes

Twin analysis, binary traits

Time to event

References

- [1] J. v. Hjelmberg, C. Fagnani, K. Silventoinen, M. McGue, M. Korkeila, K. Christensen, A. Rissanen, and J. Kaprio. Genetic influences on growth traits of BMI: a longitudinal study of adult twins. *Obesity (Silver Spring)*, 16(4):847–852, Apr 2008.
- [2] M. Korkeila, J. Kaprio, A. Rissanen, and M. Koskenvuo. Effects of gender and age on the heritability of body mass index. *Int J Obes*, 15(10):647–654, Oct 1991.