

# Package ‘lfda’

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**Type** Package

**Title** Local Fisher Discriminant Analysis

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**URL** <https://github.com/terrytangyuan/lfda>

**BugReports** <https://github.com/terrytangyuan/lfda/issues>

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**Description** Functions for performing and visualizing Local Fisher Discriminant Analysis(LFDA), Kernel Fisher Discriminant Analysis(KLFDA), and Semi-supervised Local Fisher Discriminant Analysis(SELF).

**Depends** R (>= 3.1.0)

**Imports** plyr, grDevices, rARPACK

**Suggests** testthat, rgl

**RoxygenNote** 5.0.1

**NeedsCompilation** no

**Repository** CRAN

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Cols	<i>Assigning Colors to A Vector</i>
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### Description

This function assigns a color to each distinct value in the given vector.

### Usage

```
Cols(vec)
```

### Arguments

vec                    The vector where each distinct value will be assigned a color.

### Value

The colors for each element in the given vector

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getAffinityMatrix	<i>Get Affinity Matrix</i>
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### Description

This function returns an affinity matrix within knn-nearest neighbors from the distance matrix.

### Usage

```
getAffinityMatrix(distance2, knn, nc)
```

### Arguments

distance2            The distance matrix for each observation  
knn                    The number of nearest neighbors  
nc                     The number of observations for data in this class

### Value

an affinity matrix - the larger the element in the matrix, the closer two data points are

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getMetricOfType	<i>Get Requested Type of Transforming Metric</i>
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**Description**

This function returns the requested type of transforming metric.

**Usage**

```
getMetricOfType(metric, eigVec, eigVal, total)
```

**Arguments**

metric	The type of metric to be requested
eigVec	The eigenvectors of the problem
eigVal	The eigenvalues of the problem
total	The number of total rows to be used for weighting denominator

**Value**

The transformation metric in requested type

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klfda	<i>Kernel Local Fisher Discriminant Analysis for Supervised Dimensionality Reduction</i>
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**Description**

Performs kernel local fisher discriminant analysis on the given data, which is the non-linear version of LFDA (see details [lfda](#)).

**Usage**

```
klfda(k, y, r, metric = c("weighted", "orthonormalized", "plain"), knn = 6,
      reg = 0.001)
```

**Arguments**

k	n x n kernel matrix. Result of the <a href="#">kmatrixGauss</a> function. n is the number of samples
y	n dimensional vector of class labels
r	dimensionality of reduced space (default: d)
metric	type of metric in the embedding space (default: 'weighted') 'weighted' — weighted eigenvectors 'orthonormalized' — orthonormalized 'plain' — raw eigenvectors
knn	parameter used in local scaling method (default: 6)
reg	regularization parameter (default: 0.001)

**Value**

list of the LFDA results:

T                    d x r transformation matrix ( $Z = t(T) * X$ )  
 Z                    r x n matrix of dimensionality reduced samples

**Author(s)**

Yuan Tang

**References**

Sugiyama, M (2007). - contain implementation Dimensionality reduction of multimodal labeled data by local Fisher discriminant analysis. *Journal of Machine Learning Research*, vol.8, 1027–1061.

Sugiyama, M (2006). Local Fisher discriminant analysis for supervised dimensionality reduction. In W. W. Cohen and A. Moore (Eds.), *Proceedings of 23rd International Conference on Machine Learning (ICML2006)*, 905–912.

Original Matlab Implementation: <http://www.ms.k.u-tokyo.ac.jp/software.html#LFDA>

**See Also**

See [lfda](#) for the linear version.

**Examples**

```
## Not run:
## example without dimension reduction
k <- kmatrixGauss(x = trainData[,-1])
y <- trainData[,1]
r <- 26 # dimensionality of reduced space. Here no dimension reduction is performed
result <- klfda(k,y,r,metric="plain")
transformedMat <- result$Z # transformed training data
metric.train <- as.data.frame(cbind(trainData[,1],transformedMat))
colnames(metric.train)=colnames(trainData)

## example with dimension reduction
k <- kmatrixGauss(x = trainData[,-1])
y <- trainData[,1]
r <- 3 # dimensionality of reduced space
result <- klfda(k,y,r,metric="plain")
transformMat <- result$T # transforming matrix - distance metric

# transformed training data with Style
transformedMat <- result$Z # transformed training data
metric.train <- as.data.frame(cbind(trainData[,1],transformedMat))
colnames(metric.train)[1] <- "Style"

# transformed testing data with Style (unfinished)
metric.test <- kmatrixGauss(x = testData[,-1])
```

```
metric.test <- as.matrix(testData[,-1]) %**% transformMat
metric.test <- as.data.frame(cbind(testData[,1],metric.test))
colnames(metric.test)[1] <- "Style"

## End(Not run)
```

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kmatrixGauss	<i>Gaussian Kernel Computation (Particularly used in Kernel Local Fisher Discriminant Analysis)</i>
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### Description

Gaussian kernel computation for klfda, which maps the original data space to non-linear and higher dimensions.

### Usage

```
kmatrixGauss(x, sigma = 1)
```

### Arguments

x	n x d matrix of original samples. n is the number of samples.
sigma	dimensionality of reduced space. (default: 1)

### Value

K n x n kernel matrix. n is the number of samples.

### Author(s)

Yuan Tang

### References

Sugiyama, M (2007). Dimensionality reduction of multimodal labeled data by local Fisher discriminant analysis. *Journal of Machine Learning Research*, vol.8, 1027–1061.

Sugiyama, M (2006). Local Fisher discriminant analysis for supervised dimensionality reduction. In W. W. Cohen and A. Moore (Eds.), *Proceedings of 23rd International Conference on Machine Learning (ICML2006)*, 905–912.

<https://shapeofdata.wordpress.com/2013/07/23/gaussian-kernels/>

### See Also

See klfda for the computation of kernel local fisher discriminant analysis

**Examples**

```
## Not run:
k <- kmatrixGauss(x = train.data)

## End(Not run)
```

---

lfda	<i>Local Fisher Discriminant Analysis for Supervised Dimensionality Reduction</i>
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**Description**

Performs local fisher discriminant analysis (LFDA) on the given data.

**Usage**

```
lfda(x, y, r, metric = c("orthonormalized", "plain", "weighted"), knn = 5)
```

**Arguments**

x	n x d matrix of original samples. n is the number of samples.
y	length n vector of class labels
r	dimensionality of reduced space (default: d)
metric	type of metric in the embedding space (no default) 'weighted' — weighted eigenvectors 'orthonormalized' — orthonormalized 'plain' — raw eigenvectors
knn	parameter used in local scaling method (default: 5)

**Details**

LFDA is a method for linear dimensionality reduction that maximizes between-class scatter and minimizes within-class scatter while at the same time maintain the local structure of the data so that multimodal data can be embedded appropriately. Its limitation is that it only looks for linear boundaries between clusters. In this case, a non-linear version called kernel LFDA will be used instead. Three metric types can be used if needed.

**Value**

list of the LFDA results:

T	d x r transformation matrix ( $Z = x * T$ )
Z	n x r matrix of dimensionality reduced samples

**Author(s)**

Yuan Tang

## References

Sugiyama, M (2007). Dimensionality reduction of multimodal labeled data by local Fisher discriminant analysis. *Journal of Machine Learning Research*, vol.8, 1027–1061.

Sugiyama, M (2006). Local Fisher discriminant analysis for supervised dimensionality reduction. In W. W. Cohen and A. Moore (Eds.), *Proceedings of 23rd International Conference on Machine Learning (ICML2006)*, 905–912.

## See Also

See [k1fda](#) for the kernelized variant of LFDA (Kernel LFDA).

## Examples

```
## Not run:
## example without dimension reduction
k <- trainData[,-1]
y <- trainData[,1]
r <- 26 # dimensionality of reduced space. Here no dimension reduction is performed
result <- lfda(k,y,r,metric="plain")
transformedMat <- result$Z # transformed training data
metric.train <- as.data.frame(cbind(trainData[,1],transformedMat))
colnames(metric.train)=colnames(trainData)

## example with dimension reduction
k <- trainData[,-1]
y <- trainData[,1]
r <- 3 # dimensionality of reduced space

result <- lfda(k,y,r,metric="weighted")
transformMat <- result$T # transforming matrix - distance metric

# transformed training data with Style
transformedMat <- result$Z # transformed training data
metric.train <- as.data.frame(cbind(trainData[,1],transformedMat))
colnames(metric.train)[1] <- "Style"

# transformed testing data with Style
metric.test <- as.matrix(testData[,-1]) %*% transformMat
metric.test <- as.data.frame(cbind(testData[,1],metric.test))
colnames(metric.test)[1] <- "Style"

## End(Not run)
```

**Description**

This function plot 3 dimensions of the lfda/klfda result.

**Usage**

```
## S3 method for class 'lfda'
plot(x, labels, cleanText = FALSE, ...)
```

**Arguments**

x	The lfda/klfda result.
labels	A list of class labels used for lfda/klfda training.
cleanText	A boolean value to specify whether to make the labels in the plot cleaner (default: FALSE)
...	Additional arguments

**See Also**

See [lfda](#) and [klfda](#) for the metric learning method used for this visualization.

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predict.lfda

*LFDA Transformation/Prediction on New Data*

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**Description**

This function transforms a data set, usually a testing set, using the trained LFDA metric

**Usage**

```
## S3 method for class 'lfda'
predict(object, newdata = NULL, type = "raw", ...)
```

**Arguments**

object	The result from lfda function, which contains a transformed data and a transforming matrix that can be used for transforming testing set
newdata	The data to be transformed
type	The output type, in this case it defaults to "raw" since the output is a matrix
...	Additional arguments

**Value**

the transformed matrix

**Author(s)**

Yuan Tang



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print.lfda	<i>Print an lfda object</i>
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**Description**

Print an lfda object

**Usage**

```
## S3 method for class 'lfda'  
print(x, ...)
```

**Arguments**

x	The result from lfda function, which contains a transformed data and a transforming
...	ignored

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repmat	<i>Matlab-Syntaxed Repmat</i>
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**Description**

This function mimics the behavior and syntax of repmat() in Matlab it generates a large matrix consisting of an N-by-M tiling copies of A

**Usage**

```
repmat(A, N, M)
```

**Arguments**

A	original matrix to be used as copies
N	the number of rows of tiling copies of A
M	the number of columns of tiling copies of A

**Value**

matrix consisting of an N-by-M tiling copies of A

---

self *Semi-Supervised Local Fisher Discriminant Analysis(SELF) for Semi-Supervised Dimensionality Reduction*

---

## Description

Performs semi-supervised local fisher discriminant analysis (SELF) on the given data. SELF is a linear semi-supervised dimensionality reduction method smoothly bridges supervised LFDA and unsupervised principal component analysis, by which a natural regularization effect can be obtained when only a small number of labeled samples are available.

## Usage

```
self(X, Y, beta = 0.5, r, metric = c("orthonormalized", "plain",
  "weighted"), kNN = 5, minObsPerLabel = 5)
```

## Arguments

X	n x d matrix of original samples. n is the number of samples.
Y	length n vector of class labels
beta	degree of semi-supervisedness (0 <= beta <= 1; default is 0.5 ) 0: totally supervised (discard all unlabeled samples) 1: totally unsupervised (discard all label information)
r	dimensionality of reduced space (default: d)
metric	type of metric in the embedding space (no default) 'weighted' — weighted eigenvectors 'orthonormalized' — orthonormalized 'plain' — raw eigenvectors
kNN	parameter used in local scaling method (default: 5)
minObsPerLabel	the minimum number observations required for each different label(default: 5)

## Value

list of the SELF results:

T	d x r transformation matrix ( $Z = x * T$ )
Z	n x r matrix of dimensionality reduced samples

## Author(s)

Yuan Tang

## References

Sugiyama, Masashi, et al (2010). Semi-supervised local Fisher discriminant analysis for dimensionality reduction. *Machine learning* 78.1-2: 35-61.

Sugiyama, M (2007). Dimensionality reduction of multimodal labeled data by local Fisher discriminant analysis. *Journal of Machine Learning Research*, vol.8, 1027–1061.

Sugiyama, M (2006). Local Fisher discriminant analysis for supervised dimensionality reduction. In W. W. Cohen and A. Moore (Eds.), *Proceedings of 23rd International Conference on Machine Learning (ICML2006)*, 905–912.

## See Also

See [lfda](#) for LFDA and [klfda](#) for the kernelized variant of LFDA (Kernel LFDA).

## Examples

```
## Not run:
X <- iris[,-5]
Y <- iris[,5]
result <- self(X,Y,beta = 0.1, r = 3, metric = "plain")

## End(Not run)
```

---

%^%

*Negative One Half Matrix Power Operator*

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## Description

This function defines operation for negative one half matrix power operator

## Usage

```
x %^^ n
```

## Arguments

x	the matrix we want to operate on
n	the exponent

## Value

the matrix after negative one half power

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