Package ‘deGradInfer’

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Title Parameter Inference for Systems of Differential Equation

Version 1.0.1

Description Efficient Bayesian parameter inference for systems of ordinary differential equations. The inference is based on adaptive gradient matching (AGM, Dondelinger et al. 2013 <http://proceedings.mlr.press/v31/dondelinger13a.pdf>, Macdonald 2017 <http://theses.gla.ac.uk/7987/1/2017macdonaldphd.pdf>), which offers orders-of-magnitude improvements in computational efficiency over standard methods that require solving the differential equation system. Features of the package include flexible specification of custom ODE systems as R functions, support for missing variables, Bayesian inference via population MCMC.

Depends R (>= 3.3.1)

License GPL-3

Encoding UTF-8

LazyData true

Imports deSolve, gdata, gptk, graphics, stats

RoxygenNote 7.0.2

Suggests testthat, knitr, rmarkdown, ggplot2

VignetteBuilder knitr

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R topics documented:

agm ................................................................. 2
doMCMC ............................................................ 5
getODEGradient .................................................. 6
agm

Main function for adaptive gradient matching

Description

Function agm uses adaptive gradient matching to infer the parameters of a user-defined ODE system from data. For details on AGM, see e.g. Dondelinger et al. (2013), Macdonald (2017).

Usage

```r
agm(
  data,
  time,
  ode.system,
  numberOfParameters,
  noise.sd = 0.001,
  observedVariables = 1:ncol(data),
  temperMismatchParameter = FALSE,
  initialisedParameters = NULL,
  chainNum = 20,
  gpCovType = "rbf",
  saveFile = NULL,
  defaultTemperingScheme = NULL,
  maxIterations = 3e+05,
  showPlot = FALSE,
  showProgress = FALSE,
  mismatchParameterValues = NULL,
  originalSignalOnlyPositive = FALSE,
  logPrior = "Uniform",
  explicit = FALSE,
  explicitNoiseInfer = TRUE
)
```
Arguments

data
A matrix of observations of the ODE system over time. The number of rows is equal to the number time points and the number of columns is equal to the number of variables in the system.

time
A vector containing the time points at which the observations were made.

ode.system
A function describing the ODE system. See Details for more information.

numberOfParameters
A scalar specifying the number of parameters in the ODE system. If explicitly solving the ODE system, the number of parameters will (usually) be equal to the number of ODE parameters plus the number of initial conditions of the system.

noise.sd
A scalar specifying the value at which to fix the standard deviation of the observational noise. Default noise.sd=1e-3.

observedVariables
A vector specifying which variables are observed in the system. Default is observedVariables=1:ncol(data) (fully observed system).

temperMismatchParameter
Logical: whether tempering of the gradient mismatch parameter be carried out? Default is temperMismatchParameter=FALSE.

initialisedParameters
A vector containing ODE parameters at which to intialise the MCMC. Can be set as NULL to initialise with a random draw from the prior distribution. Default is initialisedParameters=NULL.

chainNum
A scalar specifying the number of parallel temperature chains. Default is chainNum=20.

gpCovType
A string specifying the choice of kernel for the Gaussian process. Currently, there are two: gpCovType="rbf" and gpCovType="sigmoidVar".

saveFile
A string specifying the path and name of the file containing the result output. Can be set as NULL to save as "AGM Results.R" to the current working directory. Default is saveFile=NULL.

defaultTemperingScheme
A string indicating which of the two default gradient mismatch parameter value ladders to use. Choices are defaultTemperingScheme="LB2" or defaultTemperingScheme="LB10". Should only be used when temperMismatchParameter=TRUE. Default is defaultTemperingScheme=NULL.

maxIterations
A scalar specifying the number of total MCMC iterations. Default is maxIterations=300000.

showPlot
Logical: whether plots of the MCMC progress should be displayed. Default is showPlot=FALSE.

showProgress
Logical: whether % completion and various parameter values should be printed to the workspace. Default is showProgress=FALSE.

mismatchParameterValues
A matrix containing user specified values for the gradient mismatch parameter. The number of rows should be equal to chainNum and the number of columns should be equal to the number of variables in the system. A typical ladder should have the largest value in the first row and the smallest value in the last row. Should only be used when defaultTemperingScheme=NULL. Default is mismatchParameterValues=NULL.
originalSignalOnlyPositive

Logical: whether all signals observed should be non-negative. When originalSignalOnlyPositive=TRUE, any negative values of the sampled interpolant will be set to zero. Default is originalSignalOnlyPositive=FALSE.

logPrior

A string specifying whether one of the default log priors for the ODE parameters should be used, or a user-specified function. Current choices for the default prior are "Uniform", "Gamma" (shape=4, rate=2) and "Mixed" (3 ODE parameters; N(mean=0, sd=0.4), N(mean=0, sd=0.4). Alternatively the user may specify a function for calculating the prior, see Details below. Default is logPrior=’Uniform’.

explicit

Logical: whether the ODE system should be explicitly solved, rather than doing gradient matching. This means that the Gaussian process model is ignored, and the ODE system is directly fitted to the observed data. Default is explicit=FALSE.

explicitNoiseInfer

Logical: whether the standard deviation of the observational noise should be inferred when using the method that explicitly solves the ODEs. Only considered when explicit=TRUE. Default is explicitNoiseInfer=TRUE.

Details

The parameters ode.system should be a function of the form f(t,X,params) where t is the time point vector for which the derivatives should be calculated, X is a T by p matrix containing the values of the variables in the system at time t, and params is a vector with the current estimated parameter values. The function should return a matrix with the derivatives of x with respect to time (in the same order as in x). Note that in order to be consistent with the ode in package deSolve, we require that the function also works for input at a single time point.

For specifying a custom prior on the parameters, the user should write their function to take as input a vector of parameters, and return a vector of log densities for a given parameter set. For example, logPrior = function(params) c(dgamma(params,1,1,log=TRUE) defines a Gamma parameter prior with shape and scale 1.

Value

Function returns a list with elements posterior.mean, the mean of the parameter samples from the posterior (after burning of 1/4 of the number of samples taken), posterior.sd, the standard deviation, posterior.samples, the parameter samples, ll, the log likelihood, x.samples, the samples of the latent variables, gp.samples, the samples of the GP hyperparameters, noise.samples, the samples of sigma (currently fixed), swappedChains, the number of times the chains have been swapped, ll.all.chain, the log likelihood for all chains and tuning, the inferred tuning parameters for acceptance of the MCMC moves.

Examples

dataTest <- LV_example_dataset$data
timeTest <- LV_example_dataset$time
noiseTest <- LV_example_dataset$noise
doMCMC

LV_func = function(t, X, params) {
  dxdt = cbind(
    X[,1]*(params[1] - params[2]*X[,2]),
    - X[,2]*(params[3] - params[4]*X[,1])
  )
  return(dxdt)
}

# Example run only; to achieve convergence the number of iterations and
# chains must be increased.
param.result = agm(data=dataTest,time=timeTest,noise.sd=0.31,ode.system=LV_func,
  numberOfParameters=4,temperMismatchParameter=TRUE,
  chainNum=4, maxIterations=150,originalSignalOnlyPositive=TRUE,
  logPrior="Gamma",defaultTemperingScheme="LB10")

print(param.result$posterior.mean)

---

doMCMC

Main MCMC function Runs the MCMC for the specified number of
iterations and returns the sampled parameter values

Description

Main MCMC function Runs the MCMC for the specified number of iterations and returns the sampled parameter values

Usage

doMCMC(timePoints, data, auxVars, options)

Arguments

timePoints Measured time points for the ODE system.
data Observed data.
auxVars Auxiliary variables.
options Options for MCMC run.

Value

Function returns a list with elements parameters, the sampled ODE parameters for the current MCMC iteration, tuning, the inferred tuning parameters for acceptance of the MCMC moves, paramsRec, the sampled ODE parameters recorded over all MCMC iterations, lLRec, the log likelihood recorded over all MCMC iterations, xRec, the samples from the Gaussian process of the latent variables recorded over all MCMC iterations, gpRec, the samples of the hyperparameters for the Gaussian process recorded over all MCMC iterations, timePoints, the time points, noiseRec, the standard deviation of the observational noise recorded over all MCMC iterations (currently fixed), swappedChains, the number of times the chains have been swapped, chainNums, the number of...
chains, maxIterations, the total number of MCMC iterations and lLAllChains, the log likelihood for all chains recorded over all MCMC iterations. If the user specifies temperMismatchParameter=FALSE, the function additionally returns gradientMismatchParameterRec, the sampled gradient mismatch parameters recorded over all MCMC iterations.

---

**getODEGradient**  
*Calculate gradients from ODE system*

**Description**  
Calculate gradients from ODE system

**Usage**  
getODEGradient(X, timePoints, params, auxVars, species = 1:dim(X)[2])

**Arguments**

- **X**: Latent values for the species
- **timePoints**: Times at which to calculate the ODE gradients
- **params**: Current parameter estimates
- **auxVars**: Auxiliary variables (including function for ODE gradients)
- **species**: Which species to return (default=all)

**Value**  
A T by length(species) matrix with the gradients calculated at each time point for the specified species.

---

**LV_example_dataset**  
*Data from a Lotka-Volterra ODE system with 2 species and 4 parameters. Species in order are: 1. Sheep (Prey) 2. Wolves (Predators)*

**Description**

Data from a Lotka-Volterra ODE system with 2 species and 4 parameters. Species in order are: 1. Sheep (Prey) 2. Wolves (Predators)

**Usage**

LV_example_dataset
proposeParamsMCMC

Format

A list with 5 components

data Observed species with observation noise.
data.true Observed species without observation noise.
time Observed time points.
params Observed parameters.
noise Variance for the Gaussian observation noise.

Source

Generated by function simulateLotkaVolterraModel.

Description

Sample from proposal distribution for MCMC

Usage

proposeParamsMCMC(oldParams, inferredParams, width)

Arguments

oldParams Previous parameter values
inferredParams Proposed parameter values
width Width of random walk proposal

Value

List with proposed parameters, indicator variable of which parameters have changed, old and new proposal probabilities (if
sigmoidVarKernCompute  Compute K(x, x2) for sigmoid kernel, used by gptk

Description
Compute K(x, x2) for sigmoid kernel, used by gptk

Usage
sigmoidVarKernCompute(kern, x, x2 = NULL)

Arguments
- kern: kernel
- x: input 1
- x2: input 2

Value
K(x, x2)

sigmoidVarKernDiagCompute
Compute diagonal of sigmoid kernel (used by gptk).

Description
Compute diagonal of sigmoid kernel (used by gptk).

Usage
sigmoidVarKernDiagCompute(kern, x)

Arguments
- kern: Kernel
- x: Input

Value
Diagonal of the kernel
**sigmoidVarKernExpandParam**

*Insert parameters into sigmoid kernel (used by gptk)*

**Description**

Insert parameters into sigmoid kernel (used by gptk)

**Usage**

```r
sigmoidVarKernExpandParam(kern, params)
```

**Arguments**

- **kern**: kernel
- **params**: parameters

**Value**

kernel

**sigmoidVarKernExtractParam**

*Auxiliary function for sigmoid kernel (used by gptk)*

**Description**

Auxiliary function for sigmoid kernel (used by gptk)

**Usage**

```r
sigmoidVarKernExtractParam(kern, only.values = TRUE, untransformed.values = TRUE)
```

**Arguments**

- **kern**: kernel
- **only.values**: return values only
- **untransformed.values**: transform values

**Value**

hyperparameters of the GP kernel
**sigmoidVarKernGradient**

*Compute gradient of sigmoid kernel with respect to each parameter (used by gptk)*

**Description**

Compute gradient of sigmoid kernel with respect to each parameter (used by gptk)

**Usage**

```
sigmoidVarKernGradient(kern, x, x2, covGrad)
```

**Arguments**

- **kern**: kernel
- **x**: input 1
- **x2**: input 2
- **covGrad**: gradient of covariance function

**Value**

\[ \frac{dk(x, x2)}{d \theta} \]

---

**sigmoidVarKernParamInit**

*Auxiliary function for sigmoid kernel (used by gptk)*

**Description**

Auxiliary function for sigmoid kernel (used by gptk)

**Usage**

```
sigmoidVarKernParamInit(kern)
```

**Arguments**

- **kern**: GP kernel

**Value**

initialized kernel
solveODE

Solve ODE system explicitly.

Description

Solve ODE system explicitly.

Usage

solveODE(num.species, timePoints, ode.system, params)

Arguments

- num.species: Number of variables (species) in the system.
- timePoints: Time points at which to evaluate the ODE system.
- ode.system: Function for calculating the derivatives of the ODE system.
- params: Current values for the ODE parameter estimates.

Value

A list with two elements: x contains the results of integrating the ODE at the given time points, and error flags if there has been an error while invoking deSolve.
Index

*Topic datasets
   LV_example_dataset, 6

agm, 2

doMCMC, 5

getODEGradient, 6

LV_example_dataset, 6

proposeParamsMCMC, 7

sigmoidVarKernCompute, 8
sigmoidVarKernDiagCompute, 8
sigmoidVarKernExpandParam, 9
sigmoidVarKernExtractParam, 9
sigmoidVarKernGradient, 10
sigmoidVarKernParamInit, 10
solveODE, 11