

# Package ‘FCGR’

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**Type** Package

**Title** Fatigue Crack Growth in Reliability

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**Description** Fatigue Crack Growth in Reliability estimates the distribution of material lifetime due to mechanical fatigue efforts. The FCGR package provides simultaneous crack growth curves fitting to different specimens in materials under mechanical stress efforts. Linear mixed-effects models (LME) with smoothing B-Splines and the linearized Paris-Erdogan law are applied. Once defined the fail for a determined crack length, the distribution function of failure times to fatigue is obtained. The density function is estimated by applying nonparametric binned kernel density estimate (bkde) and the kernel estimator of the distribution function (kde). The results of Pinheiro and Bates method based on nonlinear mixed-effects regression (nlme) can be also retrieved. The package contains the crack.growth, PLOT.cg, IB.F, and Alea.A (database) functions.

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## R topics documented:

FCGR-package . . . . .	2
Alea.A . . . . .	3
cracks.growth . . . . .	4
IB.F . . . . .	6
PLOT.cg . . . . .	8

<b>Index</b>	<b>11</b>
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FCGR-package	<i>Fatigue Crack Growth in Reliability</i>
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### Description

Fatigue Crack Growth in Reliability estimates the distribution of material lifetime due to mechanical fatigue efforts. The FCGR package provides simultaneous crack growth curves fitting to different specimens in materials under mechanical stress efforts. Linear mixed-effects models (LME) with smoothing B-Splines and the linearized Paris-Erdogan law are applied. Once defined the fail for a determined crack length, the distribution function of failure times to fatigue is obtained. The density function is estimated by applying nonparametric binned kernel density estimate (bkde) and the kernel estimator of the distribution function (kde). The results of Pinheiro and Bates method based on nonlinear mixed-effects regression (nlme) can be also retrieved. The package contains the crack.growth, PLOT.cg, IB.F, and Alea.A (database) functions.

### Details

```

Package: FCGR
Type: Package
Version: 1.0
Date: 2015-09-29
License: GPL >= 2

```

The main functions and data frame are cracks.growth, IB.F, PLOT.cg, Alea.A

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### References

Meeker, W., Escobar, L. (1998) Statistical Methods for Reliability Data. John Wiley & Sons, Inc. New York.

Pinheiro JC., Bates DM. (2000) Mixed-effects models in S and S-plus. Statistics and Computing. Springer-Verlag. New York.

Paris, P.C. and Erdogan, F. (1963) A critical analysis of crack propagation laws. J. Basic Eng., 85, 528.

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Alea.A

*Crack growth of aluminum A-alloy due mechanical fatigue efforts*

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### **Description**

Crack growth of aluminum A-alloy due mechanical fatigue efforts. Alea.A is a data frame composed of 262 rows y 3 columns.

### **Format**

This data frame is composed of the following columns:

cycles 21 vectors with times or cycles corresponding to each specimen (overall 262 cycles).

cracks 21 vectors with the crack lengths corresponding to each specimen.

sample 21 different specimens, each one repeated the number of elements of "cycles" or "cracks".

### **Details**

Alea.A is composed of the crack length growth and number of cycles of 21 different specimens. It is detailed in Hudak et al. (1978) and referred by Meeker and Escobar (1998) in table C.14.

### **Source**

Meeker, W., Escobar, L. (1998) Statistical Methods for Reliability Data. John Wiley & Sons, Inc. New York.

### **Examples**

```
data(Alea.A)
```

**Description**

It provides the lifetime distribution of metallic materials that fail due to the crack growth produced by mechanical fatigue efforts. The crack growth trends are fitted by linear or nonlinear mixed effects regression models in order to make predictions about the material lifetime. The lifetime is defined as the time passed before the material does not meet the specification requirements and it is conditioned by a critical crack length that induces the material failure. Three different methods can be applied to estimate the fatigue lifetime distribution: "SEP-lme\_bkde" and "SEP-lme\_kde" are nonparametric while "PB-nlme" corresponds to the parametric approach proposed by Pinheiro and Bates (2000).

**Usage**

```
cracks.growth(x, aF, T_c, method = c("SEP-lme_bkde", "SEP-lme_kde",
                                     "PB-nlme"), nMC = 5000, nBKDE = 5000, nKDE = 5000)
```

**Arguments**

x	Matrix or data frame composed of three columns: times or number of cycles, crack lengths and specimen number.
aF	Critical crack length for which the material failure is produced.
T_c	Censoring time or frequency.
method	A string of characters: "SEP-lme_bkde" (default methodology) indicates that a mixed effects linear regression model is applied to crack growth data and the lifetime density is estimated by bkde method. "SEP-lme_kde" indicates that a mixed effects linear regression model is applied to crack growth data and the lifetime distribution is estimated by kde method. "PB-nlme" indicates that a mixed effects nonlinear regression model is applied to crack growth data and the lifetime the parameters are estimated maximum likelihood methodologies, and the lifetime distribution by Monte Carlo.
nMC	Number of Monte Carlo estimates, by default 5000.
nBKDE	Number of bkde estimates, by default 5000.
nKDE	Number of kde estimates, by default 5000.

**Details**

This function provides a simultaneous fitting of crack growth data corresponding to different specimens when these are subjected to mechanical fatigue efforts. For this purpose, mixed effects linear models (lme) with B-spline smoothing are applied. Since the failure is defined at a specific critical crack length, predictions of material lifetime are obtained assuming the linearized Paris-Erdogan law and the material lifetime distribution is estimated. There are available three different techniques to estimate the lifetime distribution: the binned kernel density estimate (bkde), the kernel estimator

for the distribution function (kde) computed by Quintela del Rio and Estevez-Perez (2012), and in addition the parametric method proposed by Pinheiro and Bates (2000) based on mixed effects nonlinear regression (nlme), maximum likelihood and Monte Carlo simulation.

### Value

Return a list with the following values:

data	Data frame with the data corresponding to number of cycles, crack length, and sample.
a.F	Critical crack length.
Tc	Censoring time.
param	Data frame with the estimates of Paris law parameters: C and m
crack.est	Data frame with time, crack growth estimates, and corresponding sample or specimen.
sigma	Residual standard deviation.
residuals	Residuals resulting from the crack length fitting.
crack.pred	Data frame with time, crack growth predictions out of the experimental time interval, and corresponding sample or specimen.
F.emp	Data frame with the empirical lifetime distribution and the corresponding time: time, Fe.
bw	Bandwidth used in bkde and kde methods.
F.est	Data frame with the estimated lifetime distribution and the corresponding time: time, F.
nBKDE	Number of bkde estimates.
nKDE	Number of kde estimates.
nMC	Number of Monte Carlo estimates.

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- Meeker, W., Escobar, L. (1998) Statistical Methods for Reliability Data. John Wiley & Sons, Inc. New York.
- Pinheiro JC., Bates DM. (2000) Mixed-effects models in S and S-plus. Statistics and Computing. Springer-Verlang. New York.
- Paris, P.C. and Erdogan, F. (1963) A critical analysis of crack propagation laws. J. Basic Eng., 85, 528.

Quintela-del-Rio, A. and Estevez-Perez, G. (2012) Nonparametric Kernel Distribution Function Estimation with `kerdiest`: An R Package for Bandwidth Choice and Applications, *Journal of Statistical Software* 50(8), 1. URL <http://www.jstatsoft.org/v50/i08/>.

### Examples

```
## Not run:
## Using the Alea.A dataset
data(Alea.A)
x <- Alea.A
## Critical crack length
aF <- 1.6
## Censoring time
T_c <- 0.12
## cracks.growth function applied to Alea.A data
cg <- cracks.growth(x, aF, T_c, method = c("SEP-lme_bkde", "SEP-lme_kde",
                                         "PB-nlme"), nBKDE = 5000, nKDE = 5000, nMC = 5000)
## cracks.growth values using the "SEP-lme_bkde" by default method.
names(cg)
# [1] "data"      "a.F"      "Tc"      "param"    "crack.est"
# [6] "sigma"    "residuals" "crack.pred" "F.emp"    "bw"
#[11] "F.est"    "nBKDE"
```

## End(Not run)

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 IB.F

*Bootstrap confidence bands for fatigue lifetime*

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### Description

It performs bootstrap confidence bands for fatigue lifetime. The lifetime matrix is calculated by bootstrap resampling by means the above mentioned methodologies (see `craks.growth`). The confidence bands are estimated by the quantile based method.

### Usage

```
IB.F(z, nB, alpha = 0.05, method = c("SEP-lme_bkde", "SEP-lme_kde",
                                     "PB-nlme"))
```

### Arguments

<code>z</code>	cracks.growth object.
<code>nB</code>	Number of bootstrap resampling.
<code>alpha</code>	Confidence level.
<code>method</code>	Character string showing the distribution estimates method: "SEP-lme_bkde", "SEP-lme_kde" or "PB-nlme".

**Details**

IB.F is performed from the output of `cracks.growth` function.

**Value**

Return a list with the following values:

Mat.F.B	Matrix that contents the fatigue lifetimes corresponding to each bootstrap resampling.
I.Bootstrap	Data frame that contents the bootstrap confidence bands for lifetime distribution, at a confidence level of 95 percent (by default). It is composed by two columns corresponding to the bands limits: low, up.

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Paris, P.C. and Erdogan, F. (1963) A critical analysis of crack propagation laws. J. Basic Eng., 85, 528.

**Examples**

```
## Not run:
## Using the Alea.A dataset
data(Alea.A)
x <- Alea.A
## Critical crack length
aF <- 1.6
## Censoring time
T_c <- 0.12
## cracks.growth function applied to Alea.A data
cg <- cracks.growth(x, aF, T_c, method = c("SEP-lme_bkde", "SEP-lme_kde",
    "PB-nlme"), nBKDE = 5000, nKDE = 5000, nMC = 5000)
## z is a cracks.growth object
z <- cg
## Number of bootstrap resamplings
nB <- 100
## Application of IB.F function to cg object
ic.b <- IB.F(z, nB, alpha = 0.05, method = c("SEP-lme_bkde", "SEP-lme_kde",
    "PB-nlme"))
```

```

## ic.b values obtained by the "SEP-lme_bkde" model
names(ic.b)
# [1] "Mat.F.B"      "I.Bootstrap"
## Chart with the empirical and estimated distribution functions,
## with bootstrap confidence bands at 95
# Observations from which the distribution function is estimated
F1.F <- z$F.est[,2]
plot( ic.b$I.Bootstrap$low,F1.F, col=2, type="l", lty=2, lwd=2,
      xlim=c(0.05,0.18),
      main="Plot: distributions of failure times\n confidence intervals",
      xlab="million cycles", ylab="probability", cex.lab=1.7,
      cex.main=2, las=1)
lines(ic.b$I.Bootstrap$up, F1.F, col=2, lty=2, lwd=2)
points(z$F.est, pch=20)
points(z$F.emp, col=4, pch=20, cex=1.5)
legend("topleft", c("Empirical", "Estimated", "Bootstrap (95 percent)"),
      col=c("blue", "black", "red"), lty=c(1,1,1), pch=c(20,20,20),
      cex=1.5, bty="n")
## Graph with confidence bands
matplot(ic.b$Mat.F.B, F1.F, main="Bootstrap resampling lines",
      type="l", lwd=2, xlim=c(0.05,0.18), xlab="million cycles",
      ylab="probability", cex.lab=1.7, cex.main=2, las=1)

## End(Not run)

```

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PLOT.cg

*Fatigue Crack Growth in Reliability plots*


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## Description

It provides graphical outputs composed of the trends corresponding to the crack length growth due to mechanical fatigue, the crack length estimates by the models, crack length predictions, and lifetime distribution estimates.

## Usage

```
PLOT.cg(x)
```

## Arguments

x                      cracks.growth object

## Details

Specifically, the following graphs are provided: exploratory dataset graph, plot with the crack length estimates and predictions, residuals graph, empirical and estimated lifetime distribution plot obtained by SEP-lme\_bkde, SEP-lme\_kde or PB-nlme methods.



**Value**

Return the following values:

plot.data	Exploratory chart.
plot.pred	Plot for fatigue lifetimes estimates and predictions.
plot.F	Plot for the empirical distribution and lifetimes distribution estimates of fatigue lifetimes.
plot.resid	Residuals chart.

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**References**

Meeker, W., Escobar, L. (1998) Statistical Methods for Reliability Data. John Wiley & Sons, Inc. New York.

Pinheiro JC., Bates DM. (2000) Mixed-effects models in S and S-plus. Statistics and Computing. Springer-Verlag. New York.

Paris, P.C. and Erdogan, F. (1963) A critical analysis of crack propagation laws. J. Basic Eng., 85, 528.

**Examples**

```
## Not run:
## Using the Alea.A dataset
data(Alea.A)
x <- Alea.A
## Critical crack length
aF <- 1.6
## Censoring time
T_c <- 0.12
## cracks.growth function applied to Alea.A data
cg <- cracks.growth(x, aF, T_c, method = c("SEP-lme_bkde", "SEP-lme_kde",
"PB-nlme"), nBKDE = 5000, nKDE = 5000, nMC = 5000)
## PLOT.cg applied to cg object.
PLOT <- PLOT.cg(cg)
names(PLOT)
## [1] "plot.data" "plot.pred" "plot.F" "plot.resid"
## Exploratory chart for the Alea.A dataset
PLOT$plot.data(main = "Plot: crack growth", xlab = "million cycles",
ylab = "cracks(inches)", cex.lab=1.8,
cex.main = 2)
text(0.02, x$a.F + 0.05, "Failure", cex = 1.8)
text(0.095, 0.95, "Censoring time->", cex = 1.5)
```

```
## Plot for fatigue lifetimes estimates and predictions.
PLOT$plot.pred(xlab = "million cycles", ylab = "cracks(inches)",
  main = "Plot: crack growth, estimation and prediction\n failure times (red)",
  cex.lab = 1.8, cex.main = 1.5)
text(0.02,x$a.F+0.05, "Failure", cex = 1.8)
text(0.085,0.95, "Censoring time->", cex = 1.5)
## Plot for the empirical distribution and lifetimes distribution estimates
## of fatigue lifetimes
PLOT$plot.F(main = "Plot: distributions of failure times",
  xlab = "million cycles", ylab = "probability",
  cex.lab = 1.7, cex.main=2)
text(0.14, 0.1, "<-Censoring time", cex = 1.5)
legend("topleft", c("Empirical", "Estimated"), col = c("blue","black"),
  pch=c(20,20), cex=1.5, bty="n")
## Residuals chart.
PLOT$plot.resid(main = "Plot: residual", xlab = "fitted", ylab = "residuals",
  cex = 1.5, col = "blue", cex.lab = 1.7, cex.main = 2)

## End(Not run)
```

# Index

\*Topic **IB.F**

IB.F, [6](#)

\*Topic **PLOT.cg()**

PLOT.cg, [8](#)

\*Topic **cracks.growth**

cracks.growth, [4](#)

\*Topic **datasets**

Alea.A, [3](#)

\*Topic **package**

FCGR-package, [2](#)

[Alea.A, 3](#)

[cracks.growth, 4](#)

[FCGR-package, 2](#)

[IB.F, 6](#)

[PLOT.cg, 8](#)